

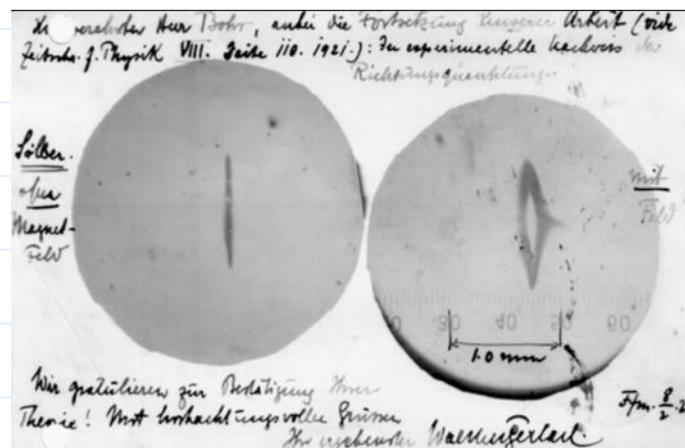
Stern-Gerlach experiment

(A6) Do the full analysis of the SG experiment.  
 Consider the experiment with needles that are magnetized.

- How would the outcome look like?
- If there's a splitting in the distribution of the needles that reach the screen, what does that imply?
- Why is it continuous in the

In the actual experiment in \_\_\_\_\_, we saw

the following pattern. What does this mean?



Postcard from Gerlach to Bohr  
 1922  
 experiment with Silver atoms  
<https://www.nature.com/articles/milespin02>



— Quantization → Do this yourselves and we talk about it later.

— Realism and Uncertainty → Commutative algebra

a)



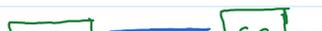
The outcome could be random.

b)



The outcome is fully deterministic. (Always up)

c)



The outcome is fully

c)



The outcome is fully random.

d)



Now if we combine (b) & (c), what would we get?

In the experiment, we get 50/50 outcomes.

What does this result imply?

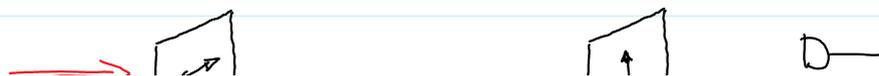
Shouldn't all the particles come out as  $x+$ ?

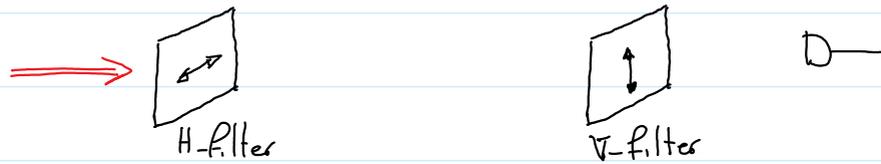
Classical Analogue: Polarization of light



Does the light reach the detector? Yes

What if we do this?





NO!

So we remove a filter & light stops going through.

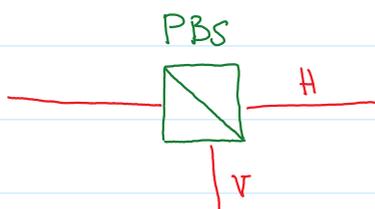
\* Think about how this experiment is related to SGE.

(A7) What's the difference?

How can we resolve the difference?

What's the classical justification of the experiment above?

Do particles of light (photons) show the same kind of behavior?



Polarizing beam-splitter:  
It lets through the horizontally polarized photon/light and



It lets through the horizontally polarized photon/light and reflects the vertically polarized photon/light.

(A8) Design an experimental setup to test (a-d) above with this PBS. (Hint: Use a polarization rotator to change the measured polarization from  $\{H \& V\}$  to  $\{\pm 45\}$ ).

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What are the implications of SG experiment?

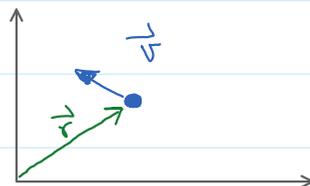
- Quantization of angular momentum or more precisely magnetic moment.

There are at least situations in which the magnetic moment has discretized values.

- No-commutativity of measurements

Contextuality  
↓  
Uncertainty

Classically:  
Example 1:



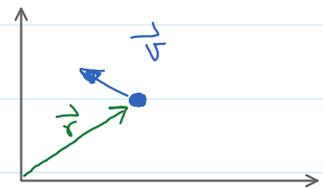
- ① What's the position?  $\vec{r}$
- ② " " velocity?  $\vec{v}$
- ③ " " position?  $\vec{r}$

The answer does not change.

$\{\vec{r}, \vec{v}\}$  are properties of (state) of the ball and not affected by the measurement

### Example 2: Angular momentum

$$\vec{L} = \vec{r} \times \vec{p} = (L_x, L_y, L_z)$$



- |   |              |                       |       |       |
|---|--------------|-----------------------|-------|-------|
| ① | What's $L_x$ | of a single particle? | $l_x$ | $l_x$ |
| ② | "            | $L_y$                 | "     | "     |
| ③ | "            | $L_x$                 | "     | "     |
- $l_x$        $l'_x \neq l_x$   
 ↑            ↑  
 Classically    suggested by SGE

Is it well-defined to talk about these properties of the system?

Can we assume that they pre-exist before the measurement?